

Time: 3 hours

Max:100 Marks

Answer ALL Questions

Part-A (10 X 2 = 20)

1. Find an iterative formula to find $\sqrt[4]{N}$ where $N \neq 0$ using Newton's method.
2. Using Gauss Jordan method find the inverse of the matrix $\begin{bmatrix} 1 & 2 \\ 2 & 3 \end{bmatrix}$.
3. State any two properties of divided difference.
4. State Newton's backward interpolation formula for equal intervals.
5. Evaluate $\int_1^{1.5} \frac{1}{x} dx$ by trapezoidal rule, dividing the range into 4 equal parts.
6. State three point Gaussian quadrature formula.
7. Using Euler's method find $y(0.2)$ from $y' = x+y$, $y(0)=1$ with $h=0.2$.
8. Write down Adams predictor, corrector formula.
9. Write down the finite difference formula for $y^1(x)$ and $y^{11}(x)$.
10. State the finite difference scheme to solve the equation $y_{tt} = \alpha^2 y_{xx}$.

PART B(5X16=80)

11 (a)(i) Solve the equation $x \sin x + \cos x = 0$ using newton-Raphson method.

(ii) Solve by Gauss Seidal iterative procedure the system

$$8x - 3y + 2z = 20, \quad 6x + 3y + 12z = 35 \quad \text{and} \quad 4x + 11y - z = 33.$$

(OR)

(b) (i) Find the real root the equation $x^3 + x^2 - 1 = 0$ by iteration method.

(ii) Using power method find the largest eigen value and the corresponding eigen

vector of the matrix $\begin{pmatrix} 1 & 6 & 1 \\ 1 & 2 & 0 \\ 0 & 0 & 3 \end{pmatrix}$.

12 (a) (i) Using Lagrange's interpolation formula find the value of y when $x=10$, if the

values of x and y are given as below:

x	5	6	9	11
y	12	13	14	16

(ii) From the following table:

x	1	2	3
y	-8	-1	18

Compute $y(1.5)$ and $y^1(1)$ using cubic spline.

(OR)

(b) (i) Using Newton's divided differences formula determine $f(3)$ from the data:

x	0	1	2	3	4
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f(x)	1	14	15	5	6
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(ii) From the data given below, find the number of students whose weight is between 60 and 70 lbs.

Wt. In lbs:	0-40	40-60	60-80	80-100	100-120
No. Of students:	250	120	100	70	50

13 (a) (i) Evaluate $\int_0^1 \frac{dx}{1+x^2}$ by using Romberg's method correct to 4 decimal places. Hence find the value of π

(ii) Evaluate $\int_0^{0.5} \int_0^0.5 \frac{\sin(xy)}{1+xy} dx dy$ using Sampson's rule with $h=k=0.25$.

(OR)

(b) (i) Find $\frac{dy}{dx}$ and $\frac{d^2y}{dx^2}$ at $x=51$, from the following data:

x	50	60	70	80	90
f(x)	19.96	36.65	58.81	77.21	94.61

(ii) Use 4 Gaussian three point formula and evaluate $\int_1^5 \frac{1}{x} dx$.

14 (a) (i) Solve $y'' = xy' - y$ given $y(0)=3, y'(0)=0$ to find the value of $y(0.1)$, using R-K method of order 4.

(ii) Using Adams method find $y(1.4)$ given $y' = x^2(1+y), y(1)=1, y(1.1)=1.233, y(1.2)=1.548$ and $y(1.3)=1.979$.

(OR)

(b) (i) Using Taylor series method solve $\frac{dy}{dx} = x^2 - y, y(0)=1$ at $x=0.1, 0.2, 0.3$. Also compare the values with the exact solution,

(ii) Given $\frac{dy}{dx} = \frac{1}{x+y}, y(0)=2, y(0.2)=2.0933, y(0.4)=2.1755, y(0.6)=2.2493$, find $y(0.8)$ using Milne's method.

15 (a) (i) Solve, by finite difference method, the boundary value problem $y''(x) - y(x) = 0$, where $y(0)=0$ and $y(1)=1$. Taking $h=0.25$

(ii) Solve the Laplace equation $U_{xx} + U_{yy} = 0$, over the square region, satisfying the boundary conditions. $U(0,y) = 0, 0 \leq y \leq 3$

$$U(3,y) = 9+y, 0 \leq y \leq 3$$

$$U(x,0) = 3x, 0 \leq x \leq 3$$

$$U(x,3) = 4x, 0 \leq x \leq 3$$

(b) (i) Solve $\frac{\partial u}{\partial t} = \frac{1}{2} \frac{\partial^2 u}{\partial x^2}$ with the conditions $u(0,t)=0=u(4,t), u(x,0)=x(4-x)$ taking $h=1$ employing Bender-Schmidt recurrence equation. Continue the solution through 10 time steps.

- (ii) Find the pivotal values of the equation $\frac{1}{4} \frac{\partial^2 u}{\partial t^2} = \frac{\partial^2 u}{\partial x^2}$ with given conditions $u(0,t)=0=u(4,t)$, $u(x,0)=x(4-x)$ and $\frac{\partial u}{\partial t}(x,0)=0$ by taking $h=1$ for 4 time steps.

AALIM MUHAMMED SALEGH COLLEGE OF ENGINEERING

Department of Mathematics

MODEL EXAMINATION MARCH 2014

VI Semester B.E(ECE).

MA2264 – NUMERICAL METHODS

Time: 3 hours

Max:100 Marks

Answer ALL Questions

Part-A (10 X 2 = 20)

1. Give the order of convergence of the Newton-Raphson method.
2. What is the condition for convergence of Gauss-Seidal method of iteration?
3. What is the Lagrange's formula to find y , if three sets of values (x_0, y_0) , (x_1, y_1) , (x_2, y_2) are given.
4. Define Cubic Spline function.
5. Write down the Newton-Cote's formula for equidistant ordinates.
6. Give order of Error in the Simpson's $1/3^{\text{rd}}$ rule.
7. Find $y(0.2)$ for the equation $y' = y + e^x$, given that $y(0)=0$ by using Euler's method.
8. Give the error for Milne's Predictor formula.
9. Classify the Partial Differential Equation $u_{xx} + 2u_{xy} + 4u_{yy} = 0$, $x, y > 0$.
10. State the diagonal five point formula for solving Laplace equation.

PART B(5X16=80)

11. a(i) Using Newton's method, find the root between 0 and 1 of $x^3 = 6x-4$ correct to 2 decimals.

(ii) Using Gauss Jordan method, find the inverse of matrix $\begin{pmatrix} 1 & 2 & 6 \\ 2 & 5 & 15 \\ 6 & 15 & 46 \end{pmatrix}$

(OR)

- b. (i) Solve the following system of equations using Gauss-Seidal method:

$$10x + 2y + z = 9; \quad x + 10y - z = -22; \quad -2x + 3y + 10z = 22.$$

(ii) Find all the eigen values and eigen vectors of the matrix $\begin{pmatrix} 1 & \sqrt{2} & 2 \\ \sqrt{2} & 3 & \sqrt{2} \\ 2 & \sqrt{2} & 1 \end{pmatrix}$ using

Jacobi method.

12. a(i) Using Lagrange's formula, find the value of x when $y=20$ from the data:

$x :$	1	2	3	4
$y=f(x):$	1	8	27	64

- (ii) Using Newton's divided differences formula, find $f(x)$ from following data

and hence find $f(4)$.

x	0	1	2	5
f(x)	2	3	12	147

(Or)

b. (i) Find the values of y when x=5 using Newton's interpolating formula from the following table

x	4	6	8	10
y	1	3	8	16

(ii) Obtain the cubic spline for the following data to find y(0.5).

x	-1	0	1	2
y	-1	1	3	35

13. (a)(i) Find the first derivative of $(x)^{1/3}$ at x= 50 given the table below.

x	50	51	52	53	54	55	56
$x^{1/3}$	3.6840	3.7084	3.7325	3.7563	3.7798	3.8030	3.8259

(ii) By Trapezoidal rule, evaluate $\int_0^6 \frac{dx}{1+x}$ and check by direct integration.
(or)

b(i) The population of a certain town is given below. Find the rate of growth of the population in 1931.

Year x	1931	1941	1951	1961	1971
Population in thousands y	40.62	60.80	79.95	103.56	132.65

(ii) Using Gaussian 3 point formula, evaluate $\int_{-1}^1 (3x^2 + 5x^4) dx$

14.(a)(i) Using Modified Euler's theorem, find y(4.1) and y(4.2) if $5x \frac{dy}{dx} + y^2 - 2 = 0$; y(4)=1.

(ii) Given that $\frac{dy}{dx} = 1 + y^2$; y(0.6) = 0.6841, y(0.4) = 0.4228, y(0.2) = 0.2027, y(0)= 0. Find y(-0.2) using Milne's method.

(or)

b(i) Using R-K fourth order method of fourth order, compute y(0.7) correct to

3 decimal places if $\frac{dy}{dx} = y - x^2$, y(0.6) = 1.7379.

(ii) Using Taylor series method, find y(1.1) correct to 4 decimal places given

$\frac{dy}{dx} = xy^{1/3}$, and y(1)=1. Also compare the values with the exact solution.

15. a(i) Solve $y'' - y = 0$ with the boundary conditions y(0)=0 and y(1) = 1.

(ii) Solve $\frac{\partial^2 u}{\partial t^2} = \frac{\partial^2 u}{\partial x^2}$ $0 < x < 1$; $t > 0$ given that $u(x,0) = 0$; $\frac{\partial u}{\partial t}(x,0) = 0$

$u(0,t) = 0$ and $u(1,t) = \frac{1}{2} \sin \pi t$. Compute u(x,t) for 4 time-steps by taking $h = \frac{1}{2}$

(or)

- b. Solve the Poisson equation $u_{xx} + u_{yy} = -10(x^2 + y^2 + 10)$ over the square mesh with sides $x=0, y=0, x=3$ and $y=3$ with $u=0$ on boundary and mesh length 1 unit.

AALIM MUHAMMED SALEGH COLLEGE OF ENGINEERING

Department of Mathematics

Model Examination MARCH 2013

(COMMON TO V1 SEMESTER ECE IV SEMESTER EEE, CIVIL)

MA 2264 –Numerical Methods

Time:3.00 hours

Answer **ALL** questions

Max.Marks: 100

Part A (10 X 2=20 Marks)

1. What is the order of convergence of Newton-Raphson method.?
2. State the convergence criteria for Gauss-Seidel iterative method?
3. Write down the Lagrange formula for $(x_1, y_1), (x_2, y_2), (x_3, y_3)$.
4. State Newton's backward difference formula.
5. State the Simpson's 3/8 rd rule.
6. State the three point Gaussian quadrature formula.
7. Write the Runge –Kutta formula for second order differential equation.
8. State Milne's predictor- corrector formula and its Error.
9. State the finite difference formula to find second order derivative with error terms.
10. State standard five point difference formula for solving $u_{xx} + u_{yy} = 0$.

PART-B (5 x 16 = 80 marks)

- 11.a) By Newton's method, find the positive root of $x^3 - x^2 - 2 = 0$ correct to three decimal places.

- b) By Gauss – elimination method, Solve

$$3x - y + 2z = 12, \quad x + 2y + 3z = 11, \quad 2x - 2y - z = 2.$$

(OR)

- c) By Gauss-Jordan method, find the inverse of the matrix

$$A = \begin{pmatrix} 6 & -2 & 2 \\ -2 & 3 & -1 \\ 2 & -1 & 3 \end{pmatrix}$$

- d) Find the numerically largest eigen value of $A = \begin{pmatrix} 25 & 1 & 2 \\ 1 & 3 & 0 \\ 2 & 0 & -4 \end{pmatrix}$

by power method and the corresponding eigen vector (correct to three decimal places)

- 12.a) Using Newton's formula, find y when $x=27$, from the following data:

$$\begin{array}{l} x: \quad 10 \quad 15 \quad 20 \quad 25 \quad 30 \\ y: \quad 35.4 \quad 32.2 \quad 29.1 \quad 26.0 \quad 23.1 \end{array}$$

- b) Using Lagrange's formula, find the value of y when $x=35$ from the data:

$$\begin{array}{l} x: \quad 25 \quad 30 \quad 40 \quad 50 \\ y: \quad 52 \quad 67.3 \quad 84.1 \quad 94.4 \end{array}$$

(OR)

c) Fit a natural cubic spline for the following data

x :	0	1	2	3
$f(x)$:	1	2	33	244

and compute $y(2.5)$

13.a) Using Numerical differentiation, find the value of $\sec 31^\circ$ from the data:

θ :	31	32	33	34
$\tan\theta$:	0.6008	0.6249	0.6494	0.6745

b) By Simpson's rule, evaluate $\int_0^2 \frac{dx}{1+x^3}$ by dividing (0,2) into 8 equal parts.

(OR)

c) Evaluate $\int_0^1 \int_0^1 \frac{2xy}{(1+x^2)(1+y^2)} dy dx$ with $h=k=0.25$ using

(i) the trapezoidal rule (ii) the Simpson's rule

14. a) Using Taylor's series method, obtain $y(0.2)$ and $y(0.4)$ if $y(x)$ satisfies

$$\frac{dy}{dx} = y - x^2 ; y(0) = 1$$

b) Given $\frac{dy}{dx} = x^2 - y$ with

x :	0	0.2	0.4	0.6
y :	0	0.02	0.0795	0.1762

using Euler's method compute $y(0.8)$ and Milne's Predictor-corrector method $y(1.0)$.

(OR)

c) Using R-K fourth order method, compute $y(0.1)$ and $y(0.2)$ if $y(x)$ satisfies

$$\frac{dy}{dx} = x + yx^2 ; y(0) = 1$$

d) Given $\frac{dy}{dx} = x^2 - y$ with

x :	0	0.1	0.2	0.3
y :	1	0.90516	0.82127	0.74918

Find $y(0.4)$ using Adam's method.

15. a) Solve the Poisson equation $u_{xx} + u_{yy} = -81xy$, $0 < x < 1$; $0 < y < 1$ given that

$$u(0, y) = 0 ; u(x, 0) = 0 ; u(1, y) = 100 ; u(x, 1) = 100 \text{ and } h = 1/3$$

b) Solve $\frac{\partial u}{\partial t} = \frac{\partial^2 u}{\partial x^2}$ in $0 < x < 5$; $t > 0$ given that $u(x, 0) = 20$; $u(0, t) = 0$; $u(5, t) = 100$.

Compute u for one time step with $h=1$ by Crank-Nicholson method.

(OR)

c) Solve $xy'' + y = 0$, $y(1)=1, y(2)=2$ with $h=0.25$ by using finite difference method.

d) Solve the $u_{xx} + u_{yy} = 0$ the square $0 \leq x, y \leq 4$ and the

boundary conditions being given as, $u=0$ at $x=0$, $u=8+2y$ at $x=4$, $u=x^2/2$ at $y=0$ and $u=x^2$ at $y=4$. with $h=k=1$.

